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Reg. No.:

Question Paper Code: 25141

B.E./B.Tech. DEGREE EXAMINATION, NOVEMBER/DECEMBER 2018.

Third Semester

Civil Engineering

#### MA 8353 - TRANSFORMS AND PARTIAL DIFFERENTIAL EQUATIONS

(Common to: Electrical and Electronics Engineering / Industrial Engineering and Management / Chemical and Electrochemical Engineering / Aeronautical Engineering / Agriculture Engineering / Automobile Engineering / Electronics and Instrumentation Engineering / Industrial Engineering / Instrumentation and Control Engineering / Manufacturing Engineering / Marine Engineering / Material Science and Engineering / Mechanical Engineering / Mechanical Engineering (Sandwich) / Mechanical and Automation Engineering / Mechatronics Engineering / Production Engineering / Robotics and Automation Engineering / Bio Technology/ Food Technology and Pharmaceutical Technology)

(Regulations 2017)

Time: Three hours

Maximum: 100 marks

Answer ALL questions.

PART A -  $(10 \times 2 = 20 \text{ marks})$ 

- 1. What are singular integrals? How does it differ from particular integral?
- 2. Solve  $2\frac{\partial^2 z}{\partial x^2} + 5\frac{\partial^2 z}{\partial x \partial y} + 2\frac{\partial^2 z}{\partial y^2} = 0$ .
- 3. What is the behavior of Fourier series of a function f(x) at the point of discontinuity?
- 4. Sketch the even and odd extensions of the periodic function  $f(x) = x^2$  for 0 < x < 2.
- 5. Classify the partial differential equation  $2x \frac{\partial^2 u}{\partial x^2} + 4x \frac{\partial^2 u}{\partial x \partial y} + 8x \frac{\partial^2 u}{\partial y^2} = 0$
- Mention the various possible general solutions for one dimensional heat equation.
- 7. Does Fourier sine transform of  $f(x) = k, 0 \le x \le \infty$ , exist? Justify your answer.

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					BOOK TO T	
	8.	State	e conv	olution theorem for Fourier transforms.		
	9.			the applications of Z-Transform?		
	10.			Transform of $f(n) = (n+1)^2$ .		
				PART B — $(5 \times 16 = 80 \text{ marks})$		
	11.	(a)	(i)	Form the partial differential equation by eliminating the arbifunction from $f(x^2 + y^2, z - xy) = 0$ .	itrary (8)	
			(ii)	Find the solution of the partial differential equation		
•				$\frac{\partial^2 z}{\partial x^2} - 4x \frac{\partial^2 z}{\partial x \partial y} + 4 \frac{\partial^2 z}{\partial y^2} = e^{2x+y}.$	(8)	
				, Or		
		(b)	(i)	Solve the Lagrange's linear equation $(x^2 - yz) p + (y^2 - zx) q = z^2 - xy.$	(8)	
			(ii)	Solve the partial differential equation		
				$(D^2 + 2DD' + D'^2 - 2D - 2D')z = \sin(x + 2y).$	(8)	
	12.	(a)	(i)	Obtain the Fourier series of the periodic function $f(x) = e^{\alpha x}$ interval $0 \le x \le 2\pi$ .		
			(ii)	Develope the Fourier series for the function $f(x) = \begin{cases} 1 + \frac{2x}{\pi}, & -\pi \le 1 \\ 1 - \frac{2x}{\pi}, & 0 \le 1 \end{cases}$	$x \le 0$ $x \le \pi$	
				Hence deduce that $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$ .	(8)	
				Or		
		(b)	(i)	Find the complex form of the Fourier series for $f(x) = e^{-1} \le x \le 1$ .	x, in (8)	
			(ii)	Develope the half range Fourier series for the function $f(x) = (0, L)$ .	x <sup>3</sup> in (8)	
	13.	(a)	(i)	Using the method of separation of variables solve $\frac{\partial u}{\partial x} = 2\frac{\partial u}{\partial t} + \frac{\partial u}{\partial t}$	и,	
				where $u(x,0) = 6e^{-3x}$ .	(8)	
			(ii)	Find the temperature $u(x,t)$ in a laterally insulated conducting bar of length $L$ with its ends kept at $0^{\circ}$ and with		
				initial temperature in the bar is $u(x,0) = 100 \sin\left(\frac{\pi x}{80}\right)$	and	
				$L = 80 \ cm.$	(8)	
				Or		
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(b)	(i) Derive the general solutions for one dimensional wave equa	ition
	$\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$ using separation of variables method.	(8)
	(ii) Find the displacement of a string stretched between two from points at a distance $L$ apart. The string is initially at resequilibrium position and points of the string are given in displacement $u(x,0) = k(Lx - x^2)$ . Assume initial velocity zero.	st in
14. (a)	(i) Find the Fourier transform of $f(x) = \begin{cases} 1 - x^2, &  x  \le 1 \\ 0, &  x  \ge 1 \end{cases}$ . Hence de-	duce
	$\int_0^\infty \frac{x \cos x - \sin x}{x^3} \cos \left(\frac{x}{2}\right) dx.$	(10)
	(ii) Construct the Fourier sine transform of $f(x) = \frac{e^{-ax}}{x}$ .	(6)
	Or	
(b)	(i) Find the Fourier cosine transforms of $f(x) = e^{-ax}$ and $g(x) = e^{-ax}$	$e^{-bx}$ .
	Using these transforms and Parseval's identity show	
	$\int_0^\infty \frac{dt}{(a^2 + t^2)(b^2 + t^2)} = \frac{\pi}{2ab(a+b)}.$	(10)
	(ii) Find the Fourier transform of $f(x) = \cos x$ , $0 \le x \le 1$ .	(6)
15. (a)	(i) Form the difference equation corresponding to the family of cu	rves
	$y = ax + bx^2.$	(8)
	(ii) Find the Z transform of $u(n) = 3n - 4\sin\left(\frac{n\pi}{4}\right) + 5\alpha$ ,	and
	$u(n) = \cos\left(\frac{n\pi}{2} + \frac{\pi}{4}\right).$	(8)
	Or ,	
(b)	(i) Use convolution theorem to evaluate the inverse Z transform	m of
	$U(z) = \frac{z^2}{(z-a)(z-b)}.$	(6)
	(ii) Solve the difference equation $y_{n+2} + 6y_{n+1} + 9y_n = 2^n$ with in	itial
	conditions $y_0 = y_1 = 0$ , using Z transform.	(10)
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