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Reg. No.:						

Question Paper Code: 21522

B.E./B.Tech. DEGREE EXAMINATION, MAY/JUNE 2013.

Third Semester

Civil Engineering

MA 2211/MA 31/MA 1201 A/CK 201/10177 MA 301/080100008/080210001 — TRANSFORMS AND PARTIAL DIFFERENTIAL EQUATIONS

(Common to all branches)

(Regulation 2008/2010)

Time: Three hours

Maximum: 100 marks

Answer ALL questions.

PART A — $(10 \times 2 = 20 \text{ marks})$

- 1. State the Dirichlet's conditions for Fourier series.
- 2. What is meant by Harmonic Analysis?
- 3. Find the Fourier Sine Transform of e^{-3x} .
- 4. If $\mathfrak{J}_{t}\{f(x)\}=F(s)$, prove that $\mathfrak{J}_{t}\{f(ax)\}=\frac{1}{a}\cdot F\left(\frac{s}{a}\right)$.
- 5. Form the PDE from $(x-a)^2 + (y-b)^2 + z^2 = r^2$.
- Find the complete integral of p+q=pq.
- In the one dimensional heat equation u_t = c² · u_{xx}, what is c²?
- Write down the two dimensional heat equation both in transient and steady states.
- 9. Find Z(n).
- 10. Obtain $Z^{-1} \left[\frac{z}{(z+1)(z+2)} \right]$.

PART B — $(5 \times 16 = 80 \text{ marks})$

11. (a) (i) Find the Fourier series of x^2 in $(-\pi, \pi)$ and hence deduce that

$$\frac{1}{1^4} + \frac{1}{2^4} + \frac{1}{3^4} + \dots \frac{\pi^4}{90} \,. \tag{8}$$

(ii) Obtain the Fourier cosine series of $f(x) = \begin{cases} kx, & 0 < x < \frac{1}{2} \\ k(l-x), & \frac{1}{2} < x < l \end{cases}$ (8)

		(11)	Obtain the Fourier cosine series of $(x-1)^{-1}$, $0 < x < 1$ and hence sho	W
			that $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots = \frac{\pi^2}{6}$.	8)
2.	(a)	(i)	Find the Fourier transform of $f(x) = \begin{cases} 1, & x < a \\ 0, & x > a \end{cases}$ and hence find	ıd
			$\int_{0}^{\infty} \frac{\sin x}{x} dx.$	8)
		(ii)	TOTAL STATE OF THE	or 8)
			Or	
	(b)	(i)	The state of the s	8)
		(ii)	Evaluate $\int_{0}^{\pi} \frac{dx}{(x^2 + a^2)^2}$ using Parseval's identity.	(8)
13.	(a)	(i)	Solve: $x(y^2-z^2)p+y(z^2-x^2)q=z(x^2-y^2)$.	8)
	(4)	(ii)	V C. C. SV	8)
		120	Or	
	(b)	(i)	Solve: $z = px + qy + \sqrt{p^2 + q^2 + 1}$.	(8)
	(0)	(ii)		(8)
14.	(a)	init	ghtly stretched string between the fixed end points $x = 0$ and $x = l$ ially at rest in its equilibrium position. If each of its points is given city $kx(l-x)$, find the displacement $y(x,t)$ of the string. Or	is a
	(b)		infinitely long rectangular plate is of width 10 cm. The temperature the short edge $y = 0$ is given by	re
			$\begin{cases} 20x, & 0 < x < 5 \\ 20(10-x), 5 < x < 10 \end{cases}$ If all the other edges are kept at ze	ro
		tem	perature, find the steady state temperature at any point on it.	
15.	(a)	(i)	Find $Z(\cos n\theta)$ and hence deduce $Z(\cos \frac{n\pi}{2})$.	(8)
		(ii)	Using Z-transform solve: $y_{n+2} - 3y_{n+1} - 10y_n = 0$, $y_0 = 1$ and $y_1 = 0$	(8)
	(b)	(i)	Or	(6)
		(ii)	F _2 1	(0)
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Find the complex form of Fourier series of $\cos ax$ in $(-\pi, \pi)$, where

"a" is not an integer.